SIXTH EDITION
BEGINNING \&
INTERMEDIATE

Elayn Martin-Gay

## Beginning \& Intermediate <br> Algebra

This page intentionally left blank

# Beginning \& Intermediate Algebra 

Sixth Edition



## PEARSON

Editorial Director, Mathematics: Christine Hoag
Editor-in-Chief: Michael Hirsch
Acquisitions Editor: Mary Beckwith
Project Manager Team Lead: Christina Lepre
Project Manager: Lauren Morse
Sponsoring Editor: Matt Summers
Editorial Assistant: Megan Tripp
Development Editor: Dawn Nuttall
Program Manager Team Lead: Karen Wernholm
Program Manager: Patty Bergin
Cover and Illustration Design: Tamara Newnam
Program Design Lead: Heather Scott
Interior Design: Integra
Executive Content Manager, MathXL: Rebecca Williams
Associate Content Manager, MathXL: Eric Gregg
Senior Content Developer, TestGen: John Flanagan
Director of Course Production: Ruth Berry
Media Producer: Audra Walsh
Senior Marketing Manager: Rachel Ross
Marketing Manager: Jennifer Edwards
Marketing Assistant: Alexandra Habashi
Senior Author Support/Technology Specialist: Joe Vetere
Procurement Specialist: Carol Melville
Production Management and Composition: Integra Software Services, Pvt. Ltd.
Text Art: Scientific Illustrators
Answer Art: Integra Software Services, Pvt. Ltd.
For permission to use copyrighted material, grateful acknowledgment is made to the copyright holders on page P1 which is hereby made an extension of this copyright page.

PEARSON, ALWAYS LEARNING, and MYMATHLAB are exclusive trademarks in the U.S. and/or other countries owned by Pearson Education, Inc. or its affiliates.

Unless otherwise indicated herein, any third-party trademarks that may appear in this work are the property of their respective owners and any references to third-party trademarks, logos or other trade dress are for demonstrative or descriptive purposes only. Such references are not intended to imply any sponsorship, endorsement, authorization, or promotion of Pearson's products by the owners of such marks or any relationship between the owner and Pearson Education, Inc. or its affiliates, authors, licensees or distributors.

## Library of Congress Cataloging-in-Publication Data

Martin-Gay, K. Elayn, 1955-
Beginning \& Intermediate Algebra / Elayn Martin-Gay, University of New Orleans. - 6th edition.
pages cm
ISBN 0-13-419309-1

1. Algebra-Textbooks. I. Title.

QA152.3.M36 2017
512.9 - dc23 2015010103

Copyright © 2017, 2013, 2009 Pearson Education, Inc. or its affiliates. All Rights Reserved. Printed in the United States of America. This publication is protected by copyright, and permission should be obtained from the publisher prior to any prohibited reproduction, storage in a retrieval system, or transmission in any form or by any means, electronic, mechanical, photocopying, recording, or otherwise. For information regarding permission, request forms and the appropriate contacts within the Pearson Education Global Rights \& Permissions department, please visit www.pearsoned.com/permissions/.

$$
\begin{array}{llllllllllllll}
1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10-R R D-W-20 & 19 & 18 & 17 & 16
\end{array}
$$

This book is dedicated to my sister—Karen Martin Callac Pasch
There's not enough space on this page to write how wonderful she was while walking this earth.

She is in a better place now; and for that, I celebrate.

This page intentionally left blank

## Contents

Preface ..... xiii
Applications Index ..... xxiii
REVIEW OF REAL NUMBERS1
1.1 Study Skill Tips for Success in Mathematics ..... 2
1.2 Symbols and Sets of Numbers ..... 8
1.3 Fractions and Mixed Numbers ..... 17
1.4 Exponents, Order of Operations, Variable Expressions, and Equations ..... 26
1.5 Adding Real Numbers ..... 36
1.6 Subtracting Real Numbers ..... 44
Integrated Review-Operations on Real Numbers ..... 51
1.7 Multiplying and Dividing Real Numbers ..... 52
1.8 Properties of Real Numbers ..... 62
Chapter 1 Vocabulary Check ..... 69
Chapter 1 Highlights ..... 69
Chapter 1 Review ..... 73
Chapter 1 Getting Ready for the Test ..... 76
Chapter 1 Test ..... 76
CHAPTEF EQUATIONS, INEQUALITIES, AND PROBLEM SOLVING ..... 78
2.1 Simplifying Algebraic Expressions ..... 79
2.2 The Addition and Multiplication Properties of Equality ..... 87
2.3 Solving Linear Equations ..... 97
Integrated Review—Solving Linear Equations ..... 105
2.4 An Introduction to Problem Solving ..... 106
2.5 Formulas and Problem Solving ..... 117
2.6 Percent and Mixture Problem Solving ..... 128
2.7 Further Problem Solving ..... 140
2.8 Solving Linear Inequalities ..... 147
Chapter 2 Vocabulary Check ..... 159
Chapter 2 Highlights ..... 159
Chapter 2 Review ..... 164
Chapter 2 Getting Ready for the Test ..... 167
Chapter 2 Test ..... 168
Chapter 2 Cumulative Review ..... 169
CHAPTER GRAPHING ..... 171
3.1 Reading Graphs and the Rectangular Coordinate System ..... 172
3.2 Graphing Linear Equations ..... 187
3.3 Intercepts ..... 197
3.4 Slope and Rate of Change ..... 205
Integrated Review-Summary on Slope and Graphing Linear Equations ..... 219
3.5 Equations of Lines ..... 220
3.6 Functions ..... 229
Chapter 3 Vocabulary Check ..... 241
Chapter 3 Highlights ..... 241
Chapter 3 Review ..... 245
Chapter 3 Getting Ready for the Test ..... 248
Chapter 3 Test ..... 249
Chapter 3 Cumulative Review ..... 251

## CHAPTER

4SOLVING SYSTEMS OF LINEAR EQUATIONS252
4.1 Solving Systems of Linear Equations by Graphing ..... 253
4.2 Solving Systems of Linear Equations by Substitution ..... 261
4.3 Solving Systems of Linear Equations by Addition ..... 268
Integrated Review—Solving Systems of Equations ..... 275
4.4 Solving Systems of Linear Equations in Three Variables ..... 276
4.5 Systems of Linear Equations and Problem Solving ..... 283
Chapter 4 Vocabulary Check ..... 301
Chapter 4 Highlights ..... 301
Chapter 4 Review ..... 304
Chapter 4 Getting Ready for the Test ..... 306
Chapter 4 Test 307
Chapter 4 Cumulative Review ..... 308
CHAPTER EXPONENTS AND POLYNOMIALS ..... 310
5.1 Exponents ..... 311
5.2 Polynomial Functions and Adding and Subtracting Polynomials ..... 322
5.3 Multiplying Polynomials ..... 334
5.4 Special Products ..... 341
Integrated Review-Exponents and Operations on Polynomials ..... 348
5.5 Negative Exponents and Scientific Notation ..... 348
5.6 Dividing Polynomials ..... 357
5.7 Synthetic Division and the Remainder Theorem ..... 364
Chapter 5 Vocabulary Check ..... 368
Chapter 5 Highlights ..... 369
Chapter 5 Review ..... 371
Chapter 5 Getting Ready for the Test ..... 374
Chapter 5 Test ..... 375
Chapter 5 Cumulative Review ..... 376
FACTORING POLYNOMIALS ..... 378
6.1 The Greatest Common Factor and Factoring by Grouping ..... 379
6.2 Factoring Trinomials of the Form $x^{2}+b x+c$ ..... 387
6.3 Factoring Trinomials of the Form $a x^{2}+b x+c$ and Perfect Square Trinomials ..... 394
6.4 Factoring Trinomials of the Form $a x^{2}+b x+c$ by Grouping ..... 402
6.5 Factoring Binomials ..... 407
Integrated Review—Choosing a Factoring Strategy ..... 414
6.6 Solving Quadratic Equations by Factoring ..... 417
6.7 Quadratic Equations and Problem Solving ..... 426
Chapter 6 Vocabulary Check ..... 435
Chapter 6 Highlights 436
Chapter 6 Review ..... 439
Chapter 6 Getting Ready for the Test ..... 441
Chapter 6 Test ..... 442
Chapter 6 Cumulative Review ..... 442
RATIONAL EXPRESSIONS ..... 444
7.1 Rational Functions and Simplifying Rational Expressions ..... 445
7.2 Multiplying and Dividing Rational Expressions ..... 455
7.3 Adding and Subtracting Rational Expressions with Common Denominators and Least Common Denominator ..... 464
7.4 Adding and Subtracting Rational Expressions with Unlike Denominators ..... 472
7.5 Solving Equations Containing Rational Expressions ..... 478
Integrated Review—Summary on Rational Expressions ..... 485
7.6 Proportion and Problem Solving with Rational Equations ..... 486
7.7 Simplifying Complex Fractions ..... 499
Chapter 7 Vocabulary Check ..... 506
Chapter 7 Highlights ..... 506
Chapter 7 Review ..... 510
Chapter 7 Getting Ready for the Test ..... 512
Chapter 7 Test ..... 513
Chapter 7 Cumulative Review ..... 514
CHAPTER MORE ON FUNCTIONS AND GRAPHS ..... 516
8
8.1 Graphing and Writing Linear Functions ..... 517
8.2 Reviewing Function Notation and Graphing Nonlinear Functions ..... 525Integrated Review-Summary on Functions and Equations of Lines 533
8.3 Graphing Piecewise-Defined Functions and Shifting and Reflecting Graphs of Functions ..... 534
8.4 Variation and Problem Solving ..... 542
Chapter 8 Vocabulary Check ..... 551
Chapter 8 Highlights ..... 552
Chapter 8 Review ..... 554
Chapter 8 Getting Ready for the Test ..... 555
Chapter 8 Test ..... 556
Chapter 8 Cumulative Review ..... 558
CHAPTER INEQUALITIES AND ABSOLUTE VALUE ..... 559
9.1 Compound Inequalities ..... 560
9.2 Absolute Value Equations ..... 567
9.3 Absolute Value Inequalities ..... 572
Integrated Review—Solving Compound Inequalities and Absolute Value Equations and Inequalities ..... 578
9.4 Graphing Linear Inequalities in Two Variables and Systems of Linear Inequalities ..... 578
Chapter 9 Vocabulary Check ..... 587
Chapter 9 Highlights ..... 588
Chapter 9 Review ..... 590
Chapter 9 Getting Ready for the Test ..... 591
Chapter 9 Test ..... 592
Chapter 9 Cumulative Review ..... 592
CHAPTER RATIONAL EXPONENTS, RADICALS, AND COMPLEX NUMBERS ..... 595
10.1 Radicals and Radical Functions ..... 596
10.2 Rational Exponents ..... 605
10.3 Simplifying Radical Expressions ..... 612
10.4 Adding, Subtracting, and Multiplying Radical Expressions ..... 620
10.5 Rationalizing Denominators and Numerators of Radical Expressions ..... 626
Integrated Review—Radicals and Rational Exponents ..... 632
10.6 Radical Equations and Problem Solving ..... 633
10.7 Complex Numbers ..... 643
Chapter 10 Vocabulary Check ..... 650
Chapter 10 Highlights ..... 650
Chapter 10 Review ..... 654
Chapter 10 Getting Ready for the Test ..... 656
Chapter 10 Test ..... 657
Chapter 10 Cumulative Review ..... 658

## QUADRATIC EQUATIONS AND FUNCTIONS <br> 660

11.1 Solving Quadratic Equations by Completing the Square 661
11.2 Solving Quadratic Equations by the Quadratic Formula671
11.3 Solving Equations by Using Quadratic Methods ..... 681Integrated Review-Summary on Solving Quadratic Equations 690
11.4 Nonlinear Inequalities in One Variable ..... 691
11.5 Quadratic Functions and Their Graphs ..... 698
11.6 Further Graphing of Quadratic Functions ..... 706
Chapter 11 Vocabulary Check ..... 714
Chapter 11 Highlights ..... 714
Chapter 11 Review ..... 717
Chapter 11 Getting Ready for the Test ..... 718
Chapter 11 Test ..... 719
Chapter 11 Cumulative Review ..... 720
CHAPTER Exponential and Logarithmic Functions ..... 722
12
12.1 The Algebra of Functions; Composite Functions ..... 723
12.2 Inverse Functions ..... 728
12.3 Exponential Functions ..... 739
12.4 Exponential Growth and Decay Functions ..... 748
12.5 Logarithmic Functions ..... 752
12.6 Properties of Logarithms ..... 760
Integrated Review-Functions and Properties of Logarithms ..... 766
12.7 Common Logarithms, Natural Logarithms, and Change of Base ..... 767
12.8 Exponential and Logarithmic Equations and Problem Solving ..... 773
Chapter 12 Vocabulary Check ..... 779
Chapter 12 Highlights ..... 780
Chapter 12 Review ..... 783
Chapter 12 Getting Ready for the Test ..... 785
Chapter 12 Test ..... 786
Chapter 12 Cumulative Review ..... 787
CHAPTER Conic Sections ..... 790
13.1 The Parabola and the Circle ..... 791
13.2 The Ellipse and the Hyperbola ..... 800
Integrated Review—Graphing Conic Sections ..... 807
13.3 Solving Nonlinear Systems of Equations ..... 808
13.4 Nonlinear Inequalities and Systems of Inequalities ..... 813
Chapter 13 Vocabulary Check ..... 817
Chapter 13 Highlights ..... 817
Chapter 13 Review ..... 820
Chapter 13 Getting Ready for the Test ..... 821
Chapter 13 Test ..... 821
Chapter 13 Cumulative Review ..... 822
CHAPTER Sequences, Series, and the Binomial Theorem ..... 824
14.1 Sequences ..... 825
14
14.2 Arithmetic and Geometric Sequences ..... 829
14.3 Series ..... 837
Integrated Review-Sequences and Series ..... 842
14.4 Partial Sums of Arithmetic and Geometric Sequences ..... 842
14.5 The Binomial Theorem ..... 849
Chapter 14 Vocabulary Check ..... 854
Chapter 14 Highlights ..... 854
Chapter 14 Review ..... 856
Chapter 14 Getting Ready for the Test ..... 858
Chapter 14 Test ..... 858
Chapter 14 Cumulative Review ..... 859
APPENDICES
A OPERATIONS ON DECIMALS/TABLE OF PERCENT, DECIMAL, AND FRACTION EQUIVALENTS ..... 861
B REVIEW OF ALGEBRA TOPICS ..... 864
C AN INTRODUCTION TO USING A GRAPHING UTILITY ..... 889
D SOLVING SYSTEMS OF EQUATIONS BY MATRICES ..... 894
E SOLVING SYSTEMS OF EQUATIONS USING DETERMINANTS ..... 899
F MEAN, MEDIAN, AND MODE ..... 906
G REVIEW OF ANGLES, LINES, AND SPECIAL TRIANGLES ..... 908
CONTENTS OF STUDENT RESOURCES ..... 915
STUDENT RESOURCES ..... 916
sTUDY SKILLS BUILDERS ..... 916
BIGGER PICTURE-STUDY GUIDE OUTLINE ..... 925
PRACTICE FINAL EXAM ..... 930
Answers to Selected Exercises ..... A1
Index ..... I1
Photo Credits ..... P1

This page intentionally left blank

## Preface

Beginning \& Intermediate Algebra, Sixth Edition was written to provide a solid foundation in algebra for students who might not have previous experience in algebra. Specific care was taken to make sure students have the most up-to-date, relevant text preparation for their next mathematics course or for nonmathematical courses that require an understanding of algebraic fundamentals. I have tried to achieve this by writing a user-friendly text that is keyed to objectives and contains many worked-out examples. As suggested by AMATYC and the NCTM Standards (plus Addenda), real-life and real-data applications, data interpretation, conceptual understanding, problem solving, writing, cooperative learning, appropriate use of technology, number sense, estimation, critical thinking, and geometric concepts are emphasized and integrated throughout the book.

The many factors that contributed to the success of the previous editions have been retained. In preparing the Sixth Edition, I considered comments and suggestions of colleagues, students, and many users of the prior edition throughout the country.

## What's New in the Sixth Edition?

- New Getting Ready for the Test can be found before each Chapter Test. These exercises help increase student success by helping students prepare for their chapter test. The purpose of these exercises is to check students' conceptual understanding of the topics in the chapter as well as common student errors. It is suggested that students complete and check these exercises before taking a practice Chapter Test. All Getting Ready for the Test exercises are either Multiple Choice or Matching, and all answers can be found in the answer section of this text.
Video Solutions of all Getting Ready exercises can be found in MyMathLab and on the Interactive DVD Lecture Series. These video solutions contain brief explanations and reminders of material in the chapter. Where applicable, incorrect choices contain explanations.
Getting Ready for the Test exercise numbers marked in blue indicate that the question is available in Learning Catalytics.
- New Learning Catalytics is an interactive student response tool that uses students' smartphones, tablets, or laptops to engage them in more sophisticated tasks and thinking. Generate class discussion, guide your lecture, and promote peer-to-peer learning with real-time analytics. Accessible through MyMathLab, instructors can use Learning Catalytics to:
- Pose a variety of open-ended questions that help your students develop critical thinking skills.
- Monitor responses to find out where students are struggling.
- Use real-time data to adjust your instructional strategy and try other ways of engaging your students during class.
- Manage student interactions by automatically grouping students for discussion, teamwork, and peer-to-peer learning.
For Beginning \& Intermediate Algebra, Sixth Edition, new Getting Ready for the Test exercises marked in blue are available in Learning Catalytics. To search for the questions in Learning Catalytics, select Discipline: Developmental Math, and Book: Martin-Gay, Beginning \& Intermediate Algebra, 6e; or search the question library for MGCOMBO6e Ch and the chapter number. For example, search MGCOMBO6e Ch4 for questions from Chapter 4.
- New Student Success Tips Videos are 3- to 5-minute video segments designed to be daily reminders to students to continue practicing and maintaining good
organizational and study habits. They are organized in three categories and are available in MyMathLab and the Interactive Lecture Series. The categories are:

1. Success Tips that apply to any course in college in general, such as Time Management.
2. Success Tips that apply to any mathematics course. One example is based on understanding that mathematics is a course that requires homework to be completed in a timely fashion.
3. Section- or Content-specific Success Tips to help students avoid common mistakes or to better understand concepts that often prove challenging. One example of this type of tip is how to apply the order of operations to simplify an expression.

- New Key Concept Activity Lab Workbook includes Extension Exercises, Exploration Activities, Conceptual Exercises, and Group Activities. These activities are a great way to engage students in conceptual projects and exploration as well as group work.
- The Martin-Gay MyMathLab course has been updated and revised to provide more exercise coverage, including assignable video check questions and an expanded video program. There are section lectures videos for every section, which students can also access at the specific objective level; new Getting Ready for the Test video solutions; new Student Success Tips videos; and an increased number of watch clips at the exercise level to help students while doing homework in MathXL.
Vocabulary, Readiness \& Video Check Questions continue to be available in the text and for assignment in MyMathLab. The Readiness exercises center on a student's understanding of a concept that is necessary in order to continue to the exercise set. The video check questions are included in every section for every learning objective. These exercises are a great way to assess whether students have viewed and understood the key concepts presented in the videos.
- Exercise Sets Revised and Updated The text exercise sets have been carefully examined and revised. Special focus was placed on making sure that even- and odd-numbered exercises are paired and that real-life applications are updated.


## Key Continuing Resources and Pedagogical Features

Interactive DVD Lecture Series, featuring your text author Elayn Martin-Gay, provides students with active learning at their own pace. The videos offer the following resources and more:

A complete lecture for each section of the text highlights key examples and exercises from the text. Pop-ups reinforce key terms, definitions, and concepts.
An interface with menu navigation features allows students to quickly find and focus on the examples and exercises they need to review.
Interactive Concept Check exercises measure students' understanding of key concepts and common trouble spots.

New Student Success Tips Videos.

- The Interactive DVD Lecture Series also includes the following resources for test prep:


## New Getting Ready for the Chapter Test Videos

The Chapter Test Prep Videos help students during their most teachable moment-when they are preparing for a test. This innovation provides step-by-step solutions for the exercises found in each Chapter Test. For the Sixth Edition, the chapter test prep videos are also available on YouTube ${ }^{\mathrm{TM}}$. The videos are captioned in English and Spanish.

The Practice Final Exam Videos help students prepare for an end-of-course final. Students can watch full video solutions to each exercise in the Practice Final Exam at the end of this text.

- The Video Organizer is designed to help students take notes and work practice exercises while watching the Interactive Lecture Series videos (available in MyMathLab and on DVD). All content in the Video Organizer is presented in the same order as it is presented in the videos, making it easy for students to create a course notebook and build good study habits.
- Covers all of the video examples in order.
- Provides ample space for students to write down key definitions and properties.
- Includes Play and Pause button icons to prompt students to follow along with the author for some exercises while they try others on their own.

The Video Organizer is available in a loose-leaf, notebook-ready format. It is also available for download in MyMathLab. Answers to all video questions are available to instructors in MyMathLab and the Instructor's Resource Center.

## Key Pedagogical Features

The following key features have been retained and/or updated for the Sixth Edition of the text:

Problem-Solving Process This is formally introduced in Chapter 2 with a four-step process that is integrated throughout the text. The four steps are Understand, Translate, Solve, and Interpret. The repeated use of these steps in a variety of examples shows their wide applicability. Reinforcing the steps can increase students' comfort level and confidence in tackling problems.

Exercise Sets Revised and Updated The exercise sets have been carefully examined and extensively revised. Special focus was placed on making sure that even- and oddnumbered exercises are paired.

Examples Detailed, step-by-step examples were added, deleted, replaced, or updated as needed. Many examples reflect real life. Additional instructional support is provided in the annotated examples.

Practice Exercises Throughout the text, each worked-out example has a parallel Practice Exercise. These invite students to be actively involved in the learning process. Students should try each Practice Exercise after finishing the corresponding example. Learning by doing will help students grasp ideas before moving on to other concepts. Answers to the Practice Exercises are provided in the back of the text.

Helpful Hints Helpful Hints contain practical advice on applying mathematical concepts. Strategically placed where students are most likely to need immediate reinforcement, Helpful Hints help students avoid common trouble areas and mistakes.

Concept Checks This feature allows students to gauge their grasp of an idea as it is being presented in the text. Concept Checks stress conceptual understanding at the point of use and help suppress misconceived notions before they start. Answers appear at the bottom of the page. Exercises related to Concept Checks are included in the exercise sets.

Mixed Practice Exercises Found in the section exercise sets, these require students to determine the problem type and strategy needed to solve it just as they would need to do on a test.

Integrated Reviews A unique, mid-chapter exercise set that helps students assimilate new skills and concepts that they have learned separately over several sections. These
reviews provide yet another opportunity for students to work with mixed exercises as they master the topics.

Vocabulary Check Provides an opportunity for students to become more familiar with the use of mathematical terms as they strengthen their verbal skills. These appear at the end of each chapter before the Chapter Highlights. Vocabulary, Readiness, and Video Check exercises provide practice at the section level.

Chapter Highlights Found at the end of every chapter, these contain key definitions and concepts with examples to help students understand and retain what they have learned and help them organize their notes and study for tests.

Chapter Review The end of every chapter contains a comprehensive review of topics introduced in the chapter. The Chapter Review offers exercises keyed to every section in the chapter, as well as Mixed Review exercises that are not keyed to sections.

Chapter Test and Chapter Test Prep Video The Chapter Test is structured to include those problems that involve common student errors. The Chapter Test Prep Videos give students instant author access to a step-by-step video solution of each exercise in the Chapter Test.

Cumulative Review Follows every chapter in the text (except Chapter 1). Each oddnumbered exercise contained in the Cumulative Review is an earlier worked example in the text that is referenced in the back of the book along with the answer.

Writing Exercises \ These exercises occur in almost every exercise set and require students to provide a written response to explain concepts or justify their thinking.

Applications Real-world and real-data applications have been thoroughly updated, and many new applications are included. These exercises occur in almost every exercise set, show the relevance of mathematics, and help students gradually and continuously develop their problem-solving skills.

Review Exercises These exercises occur in each exercise set (except in Chapter 1) and are keyed to earlier sections. They review concepts learned earlier in the text that will be needed in the next section or chapter.

Exercise Set Resource Icons Located at the opening of each exercise set, these icons remind students of the resources available for extra practice and support:

$$
\text { MyMathLab }{ }^{\circ}
$$

See Student Resource descriptions page xvii for details on the individual resources available.

Exercise Icons These icons facilitate the assignment of specialized exercises and let students know what resources can support them.
(Dideo icon: exercise worked on the Interactive DVD Lecture Series and in MyMathLab.
$\triangle$ Triangle icon: identifies exercises involving geometric concepts.
> Pencil icon: indicates a written response is needed.
Calculator icon: optional exercises intended to be solved using a scientific or graphing calculator.

Optional: Calculator Exploration Boxes and Calculator Exercises The optional Calculator Explorations provide keystrokes and exercises at appropriate points to give an opportunity for students to become familiar with these tools. Section exercises that are best completed by using a calculator are identified by 媲 for ease of assignment.

## STUDENT RESOURCES

## Interactive DVD Lecture Series Videos

Provides students with active learning at their own pace. The videos offer:

- A complete lecture for each text section. The interface allows easy navigation to examples and exercises students need to review.
- Interactive Concept Check exercises
- Student Success Tips Videos
- Practice Final Exam
- Getting Ready for the Chapter Test Videos
- Chapter Test Prep Videos


## Video Organizer

Designed to help students take notes and work practice exercises while watching the Interactive Lecture Series videos.

- Covers all of the video examples in order.
- Provides ample space for students to write down key definitions and rules.
- Includes Play and Pause button icons to prompt students to follow along with the author for some exercises while they try others on their own.

Available in loose-leaf, notebookready format and in MyMathLab.

## Student Solutions Manual

Provides completely worked-out solutions to the odd-numbered section exercises; all exercises in the Integrated Reviews, Chapter Reviews, Chapter Tests, and Cumulative Reviews.
Key Concept Activity Lab Workbook includes Extension Exercises, Exploration Activities, Conceptual Exercises, and Group Activities.

## INSTRUCTOR RESOURCES

| Annotated Instructor's Edition <br> Contains all the content found in the student edition, plus the following: <br> - Classroom example paired to each example <br> - Answers to exercises on the same text page <br> - Teaching Tips throughout the text, placed at key points <br> - Video Answer Section | Instructor's Resource Manual with Tests and <br> Mini-Lectures <br> - Mini-lectures for each text section <br> - Additional Practice worksheets for each section <br> - Several forms of test per chapter-free response and multiple choice <br> - Answers to all items <br> Instructor's Solutions Manual <br> TestGen ${ }^{\circledR}$ (Available for download from the IRC) |
| :---: | :---: |
| Instructor-to-Instructor Videos-available in the Instructor Resources section of the MyMathLab course. | Online Resources <br> MyMathLab ${ }^{\circledR}$ (access code required) <br> MathXL ${ }^{\circledR}$ (access code required) |

## Get the most out of MyMathLab

MyMathLab is the world's leading online resource for teaching and learning mathematics. MyMathLab helps students and instructors improve results and provides engaging experiences and personalized learning for each student so learning can happen in any environment. Plus, it offers flexible and time-saving course-management features to allow instructors to easily manage their classes while remaining in complete control, regardless of course format.

## Personalized Support for Students

- MyMathLab comes with many learning resources-eText, animations, videos, and more-all designed to support your students as they progress through their course.
- The Adaptive Study Plan acts as a personal tutor, updating in real time based on student performance to provide personalized recommendations on what to work on next. With the new Companion Study Plan assignments, instructors can now assign the Study Plan as a prerequisite to a test or quiz, helping to guide students through concepts they need to master.
- Personalized Homework allows instructors to create homework assignments tailored to each student's specific needs by focusing on just the topics they have not yet mastered.

Used by nearly 4 million students each year, the MyMathLab and MyStatLab family of products delivers consistent, measurable gains in student learning outcomes, retention, and subsequent course success.

## Acknowledgments

Many people helped me develop this text, and I will attempt to thank some of them here. Cindy Trimble was invaluable for contributing to the overall accuracy of the text. Dawn Nuttall, Emily Keaton, and Suellen Robinson were invaluable for their many suggestions and contributions during the development and writing of this Sixth Edition. Courtney Slade, Chakira Lane, Patty Bergin, and Lauren Morse provided guidance throughout the production process.

A very special thank you goes to my editor, Mary Beckwith, for being there 24/7/365, as my students say. Last, my thanks to the staff at Pearson for all their support: Michael Hirsch, Rachel Ross, Heather Scott, Michelle Renda, Chris Hoag, and Paul Corey.

I would like to thank the following reviewers for their input and suggestions:
Rosalie Abraham, Florida Community College_Jacksonville
Ana Bacica, Brazosport College
Nelson Collins, Joliet Junior College
Nancy Desilet, Carroll Community College
Elizabeth Eagle, University of North Carolina-Charlotte
Dorothy French, Community College of Philadelphia
Sharda Gudehithla, Wilbur Wright College
Pauline Hall, Iowa State University
Debra R. Hill, University of North Carolina-Charlotte
Glenn Jablonski, Triton College
Sue Kellicut, Seminole State College
Jean McArthur, Joliet Junior College
Mary T. McMahon, North Central College
Owen Mertens, Missouri State University
Jeri Rogers, Seminole State College
William Stammerman, Des Moines Area Community College
Patrick Stevens, Joliet Junior College
Arnavaz Taraporevala, New York City College of Technology

I would also like to thank the following dedicated group of instructors who participated in our focus groups, Martin-Gay Summits, and our design review for the series. Their feedback and insights have helped to strengthen this edition of the text. These instructors include:

Billie Anderson, Tyler Junior College
Cedric Atkins, Mott Community College
Lois Beardon, Schoolcraft College
Laurel Berry, Bryant \& Stratton College
John Beyers, University of Maryland
Bob Brown, Community College of Baltimore County-Essex
Lisa Brown, Community College of Baltimore County-Essex
NeKeith Brown, Richland College
Gail Burkett, Palm Beach State College
Cheryl Cantwell, Seminole State College
Ivette Chuca, El Paso Community College
Jackie Cohen, Augusta State College
Julie Dewan, Mohawk Valley Community College
Monette Elizalde, Palo Alto College
Kiel Ellis, Delgado Community College
Janice Ervin, Central Piedmont Community College
Richard Fielding, Southwestern College
Dena Frickey, Delgado Community College
Cindy Gaddis, Tyler Junior College
Gary Garland, Tarrant County Community College
Kim Ghiselin, State College of Florida
Nita Graham, St. Louis Community College

Kim Granger, St. Louis Community College
Pauline Hall, Iowa State University
Pat Hussey, Triton College
Dorothy Johnson, Lorain County Community College
Sonya Johnson, Central Piedmont Community College
Ann Jones, Spartanburg Community College
Irene Jones, Fullerton College
Paul Jones, University of Cincinnati
Mike Kirby, Tidewater Community College
Kathy Kopelousous, Lewis and Clark Community College
Tara LaFrance, Delgado Community College
John LaMaster, Indiana Purdue University Fort Wayne
Nancy Lange, Inver Hills Community College
Judy Langer, Westchester Community College
Kathy Lavelle, Westchester Community College
Lisa Lindloff, McLennan Community College
Sandy Lofstock, St.Petersburg College
Nicole Mabine, North Lake College
Jean McArthur, Joliet Junior College
Kevin McCandless, Evergreen Valley College
Ena Michael, State College of Florida
Armando Perez, Laredo Community College
Davidson Pierre, State College of Florida
Marilyn Platt, Gaston College
Chris Riola, Moraine Valley Community College
Carole Shapero, Oakton Community College
Janet Sibol, Hillsborough Community College
Anne Smallen, Mohawk Valley Community College
Barbara Stoner, Reading Area Community College
Jennifer Strehler, Oakton Community College
Ellen Stutes, Louisiana State University Eunice
Tanomo Taguchi, Fullerton College
Robyn Toman, Anne Arundel Community College
MaryAnn Tuerk, Elgin Community College
Walter Wang, Baruch College
Leigh Ann Wheeler, Greenville Technical Community College
Darlene Williams, Delgado Community College
Valerie Wright, Central Piedmont Community College
A special thank you to those students who participated in our design review: Katherine Browne, Mike Bulfin, Nancy Canipe, Ashley Carpenter, Jeff Chojnachi, Roxanne Davis, Mike Dieter, Amy Dombrowski, Kay Herring, Todd Jaycox, Kaleena Levan, Matt Montgomery, Tony Plese, Abigail Polkinghorn, Harley Price, Eli Robinson, Avery Rosen, Robyn Schott, Cynthia Thomas, and Sherry Ward.
Elayn Martin-Tay

## About the Author

Elayn Martin-Gay has taught mathematics at the University of New Orleans for more than 25 years. Her numerous teaching awards include the local University Alumni Association's Award for Excellence in Teaching, and Outstanding Developmental Educator at University of New Orleans, presented by the Louisiana Association of Developmental Educators.

Prior to writing textbooks, Elayn Martin-Gay developed an acclaimed series of lecture videos to support developmental mathematics students in their quest for success. These highly successful videos originally served as the foundation material for her texts. Today, the videos are specific to each book in the Martin-Gay series. The author has also created Chapter Test Prep videos to help students during their most "teachable moment"-as they prepare for a test-along with Instructor-to-Instructor videos that provide teaching tips, hints, and suggestions for each developmental mathematics course, including basic mathematics, prealgebra, beginning algebra \& intermediate algebra. Her most recent innovations are the Algebra Prep Apps for the iPhone and iPod Touch. These Apps embrace the different learning styles, schedules, and paces of students and provide them with quality math tutoring.

Elayn is the author of 12 published textbooks as well as multimedia interactive mathematics, all specializing in developmental mathematics courses. She has participated as an author across the broadest range of educational materials: textbooks, videos, tutorial software, and courseware. This offers an opportunity of various combinations for an integrated teaching and learning package offering great consistency for the student.

This page intentionally left blank

## Applications Index

## A

Academics. See Education
Agriculture
bug spray mixtures, 497, 750
combine rental fees, 857
cranberry-producing states, 16,137
DDT pesticides, 750
farm sizes in U.S., 184, 680
farmland prices, 219
farms, number of, 138, 307
weed killer mixtures, 497
Animals \& Insects
bear populations, 784
beetle species, 114
bison populations, 751
bug sprays, $497,750,848,857$
cheetah running speeds, 461
condor populations, 785
crane births, 857
cricket chirps, 116, 126, 127
DDT pesticides, 750
dog medicine dosages, 240, 532
dog run width, 119
fish tank dividers, 638
flying fish speeds, 128
goldfish numbers in tanks, 126
gorilla births, 839
grasshopper species, 114
hyenas overtaking giraffes, 499
insecticides, 848,857
mosquitoes, $747,767,857$
opossum deaths, 841
otter births, 841
owl populations, 841
pen dimensions, $127,679,813$
pet types owned in U.S., 130
pet-related expenditures, 183
pine beetle infestations, 856
piranha fish tank dimensions, 126
prairie dog populations, 787,932
puppy weight gain, 827
rat populations, 751
sparrow populations, 828
wolf populations, 778
wood duck populations, 787
Astronomy \& Space
alignment of planets, 471
comet distance from Earth, 355
gamma ray conversion by Sun, 356
Jupiter, 373
light travel time/distance, 127-128, 356
magnitude of stars, 16-17
meteorite weights, 96,114

Milky Way, 373
moon's light reaching Earth, 357
moon's surface area, 640
orbit of planets and comets, 806-807
planet temperatures, 61
Sun's light reaching Earth, 357
telescope elevation above sea level, 355
weight of objects in relation to Earth's center, 549
weights on Earth vs. other planets, 495
Automobiles
age of, 218
bus speeds, 145, 494, 497, 498
car speeds, $145,493-494,496,497,498,511,549,640,658$
compact cars, cost of operating, 218
dealership discounts, 136
driver's licenses, 195
fatalities, 298
fuel economy, 218
motorcycle speeds, 498
registered vehicles on road, 138
sales, 228,848
traffic tickets, 146, 497
used car values, 138, 181, 554
Aviation
airplane seats, 876
airplane speed in still air, 296, 497, 498
airport elevations, 50
airport traffic, 718, 870, 877
hang glider flight rate, 128
hypersonic flight time around Earth, 128
jet $v s$. car distances, 497
jet vs. propeller plane speeds, 145, 497
runway length, 127
SpaceShipOne rocket plane speed, 463
vertical elevation changes, 50
wind speeds, 296, 496, 497, 498

## B

Business \& Industry
advertising, 220, 848
balancing company books, 498
book store closures, 228
break-even point, 147, 291-292, 299
car rental fees, 296, 587
charity donations, 845
Coca-Cola production, 137
Coca-Cola sign dimensions, 124
consulting fees, 511
Cyber Monday, 746
defective products, 514
delivery service daily operating costs, 642
depreciation of copiers, 827
diamond production, 114, 532

Business \& Industry (continued)
discounts, 131, 136, 166
downsizing, 138, 165, 168
Dunkin' Donuts stores, 228
employee age, 274
employee production numbers and hourly wages, 185
employment decline, 524, 751, 875,876
employment growth, $167,228,298,524,875$
faxes and fax machines, 848,876
food manufacturing plants, 137
gross profit margin, 454
group/bulk pricing, 287-288, 297
Home Depot revenue, 195
home prices, 524
hourly minimum wage, 238-239, 533
labor estimates, 491-492, 494, 496, 497, 498, 499, 511, 550, 684-685, 689, 691, 717, 720
laundromat prices, 213
manufacturing costs, $245,299,434,450-451,453,510$, 511, 513, 549, 713, 728, 788
manufacturing volumes, 204, 355
markup and new price, 166
NASDAQ sign dimensions, 124
net income, 43, 77
net sales, 176
occupations predicted to increase, 275
online shopping, 706, 874
original price after discount, 166
percent increase/decrease, 136, 166, 167
postage for large envelopes, 239
price and demand, 670, 813
price decrease and new price, 138,872
price per items purchased, 294, 296, 659
price to sales ratio, 524
pricing and sales relationship, 228-229, 297
profits, 228, 454, 524, 713, 728
proofreading rates, 497
quantity pricing, 184,245
restaurant employees, 874
restaurant sales, 213, 680
restaurants in U.S., 228, 524
retail sales, 706
revenue, 195, 299, 372, 453, 728, 857
salary after pay raise, 136
salary growth, $832,836,841,848,856,857$
sale prices, $137-138,224,752$
sales tax, 859
sales volume, predicting, 224-225
volume of items sold at original vs. reduced prices, 297
Walmart stores, 186
word processing, 587, 684-685
work rates, 491-492, 494, 496, 497, 498, 499, 511, 550, 684-685, 689, 691, 717, 720
years on market and profit relationship, 228

## C

Cars. See Automobiles
Chemistry
Avogadro's number, 356
eyewash stations, 134
freezing and boiling points of water, 15
gas pressure and Boyle's law, 545, 555
greenhouse gases, 746
lotion mixtures, 139
methane gas emissions, 713-714
nickel, half-life of, 752
nuclear waste, 746
pH of liquids, 760
radioactive material, $744,746,751,760,836,841,857$
solution mixtures, 133-134, 136, 138, 162, 166, 251,
290-291, 296, 297, 299, 300, 305, 307, 497, 658, 930
sulfur dioxide emissions, 516, 523
uranium, half-life of, 752
Communications \& Technology
area codes, $111,168,930$
cell phone discounts, 131
cell phone use, 78, 166, 611
computer assembly, 848
computer discounts, 872
computer rentals, 848
computer values, 180-181
country codes, 114
digital media use, 298
Dish Network subscribers, 250
email, 874
engineers, 193
faxes and fax machines, 848,876
Google searches, 373
households with computers, 195-196, 217
Internet advertising, 220
Internet crime complaints, 136
Internet usage, 166, 172, 310, 333, 680, 877
light bulbs, 877
mobile devices, time spent on, 137
music streaming, 387
newspaper circulation figures, 228
radio stations in U.S., 268
security keypads, 813
smart televisions, 787
social media, 402, 559, 577
software revenue, 372
switchboard connections, 434
television assembly, 857
Wi-Fi enabled cell phones, 713, 864, 875, 878
ZIP codes, 875
Construction \& Home Improvement
balsa wood stick lengths, 443, 658
baseboard and carpeting measurements, 124
beam lengths, 113
beams, $113,333,550$
blueprint measurements, 495
board lengths, $92,95,104,108,113,115,165,477$
board pricing, 184
building values, 554
carpet rolls, 843
column weight, 547-548, 550
computer desk length, 95
dams, 660
deck dimensions, 168, 442, 497
doors, 679
fencing, $125,251,300,873$
fertilizer needs, 126
gardens, $116,119,125,251,300,435,492,840,859$
golden ratio, 679
grass seed, 125
housing starts $v s$. housing completions, 566
ladders, 433
lawn care, 125,126
measurement conversions, 460-461, 463
molding lengths, 75, 333
painting houses, 511
picture frames, 125,876
pipe length, 656
roofing pitch, $212,217,218$
roofing time, 721
rope lengths, 93,112
sewer pipe slope, 217
siding section lengths, 115
spotlight placement, 640
sprinklers, 689
stained glass windows, 679
steel section lengths, 112
string/wire lengths, $93,95,114,115,167,433,604,640$
swimming pools, $165,321,363,435,497$
trees planted, 840
wall border, 125
washer circumference, 158
wire placement, 637-638, 640

## D

Demographics
age groups predicted to increase on workforce, 274
bill collectors, 298
birth rate in U.S., 138
child care centers, 76
driver's licenses, 195
engineers, 193
Internet usage, 166, 172, 310, 333
joggers, 195
metropolitan populations, 869,876
occupations predicted to increase, 275
octuplet birth weights, 74
pet types owned in U.S., 130
population growth, 748-749, 751, 784, 785, 787, 828, 834, 859, 876
population per square mile of land, 228
population size, 775, 778, 779, 787
postal carriers, 298
registered nurses, 192
water use per person, 250, 549
world population, 356
Distance. See Time \& Distance

## E

Economics \& Finance. See also Personal Finances coin/bill denominations, 142-143, 145, 146, 166, 294, 296, 305, 306
compound interest, 666-667, 669, 743, 747, 770, 772-773, $776,778,783,784,785,787,859,860$
interest rates, 36, 434, 666-667, 669, 670, 717, 743, 747, 770, $772-773,776,778,783,784,785,787,859,860$
investment amounts, 143-144, 145, 146, 166, 168, 295, 514
loans, money needed to pay off, 321
money problems, 142-143
national debts, 356
shares of stock owned, 296
simple interest, 145, 146
stamp denominations, 296, 306
stock market gains and losses, $61,73,75,77$
stock prices, 296
Education
ACT Assessment scores, 166, 300
admission rates, 15
alumni donations, 844
associate degrees, 246, 378
bachelor's degrees, 267-268, 378
book page numbers, 114
classrooms, 96, 114, 496
college budgeting, 155
combination lock codes, 114
desired employment benefits, 138
graduate and undergraduate student enrollment, 15, 96, 527-528, 828
high school graduates, 387
hours spent studying, 184
Internet access in classrooms, 138
IQ scores, 642
learning curves, 778
president salaries, 876
students per teacher, 183
study abroad students, 746
summer school students, 751
test scores, $158,567,875$
textbook prices, 876
tuition and fees, 132, 247
Entertainment \& Recreation
allowances, 828
auditorium seats, 836,856
card game scores, 50
casino gaming, 461
deep-sea diving, 15
diving, 15, 61
DVD sale prices, 166
Easter eggs, 158
exercise bikes, 836
Ferris wheels, 799
fund-raiser attendance, 297
gambling, 848
group rate admissions to events, 287-288
hang gliders, 128, 429
ice sculpting, 843
iTunes expenditures, 186
jogging, 195, 305, 496, 688
movie admission prices, 185,204
movie industry revenue, 183
movie patron ages, 877

Entertainment \& Recreation (continued)
movie theater screens, $26,113,133,204$
movie theater seats, 828,857
movie ticket sales, 250
museums and art galleries, 73
music CDs, 136, 450-451
music streaming, 387
national park visits, 245, 331-332, 434
Netflix growth, 722, 742-743, 746
ping-pong tables, 363
pool, 848
poster contests, 679
pyramids formed by surfers, 841
Redbox rentals, 488-489
sail dimensions, 126, 428-429, 440, 497, 515
smart televisions, 787
snowboarding, 872
summer camp tournaments, 784
swimming, 165
tickets sold by type, 145, 287-288, 305
tourism expenditures, 217
tourist destinations, 171, 182
video games, 116
zorbing, 595, 620

## F

Finance. See Economics \& Finance; Personal Finances
Food \& Nutrition
barbecues, 471
breakfast item prices, 305
calories burned while walking/bicycling, 157
calories in food items, 495, 497
candy mixtures, 300,305
cheese consumption and production, 298, 572, 746
coffee blends, 137, 297
cook preparation time, 498
dinner cost with tip, 136
drink machines, coin denominations in, 86
fishery products, domestic and imported, 252, 260
frozen yogurt store revenue, 857
fruit companies, 228
grocery store displays, 836
liter-bottles of Pepsi, 489
nut mixtures, 137, 297, 497
nutrition labels, 139
pepper hotness (Scoville units), 139
percent decrease/increase of consumption, 138
pizza sizes, 126
rabbit food mixtures, 299
red meat and poultry consumption, 283-284
restaurant sales, 213
trail mix ingredients, 139
vitamin A and body weight, 681
yogurt production, 248

## G

Geography
continent/regional percentage of Earth's land, 136
desert areas, 96, 114
earthquake magnitudes, 768-769, 772, 874
elevation, 10, 15, 42, 47, 50, 61
federally owned land, 874
Newgrange tomb, 790, 799
ponds, 494, 511, 656, 688
river length, 96
river lenth, 96
rope needed to wrap around Earth, 126
Sarsen Circle of Stonehenge, 798-799
state counties, 115
tallest buildings in U.S., 907
tornado classification, 168
volcano heights, 161
volcano surface area, 620
wildfires, 177
Geology
diamond production, 114, 532
glacier flow rates, 117-118, 128
lava flow rates, 118,127
mixtures, 138
stalactites and stalagmites, 128
Geometry
angle measurements, $15,50,74,95,96,109-110,113$, $114,115,116,293-294,297,299,300,308,478,485,649$, 875, 876
area, $24,35-36,74,127,136,138,320,332,339,340,346$, $347,356,363,368,373,374,376,387,402,432,433,440$, 464, 477, 510, 532, 546, 626, 641
billboard dimensions, 127,165
boxes/cubes, $36,122,127,320,321,339,356,368,372,532,689$
circles, 24-25, 74, 158, 320, 432, 532, 550-551
circumference, 158, 550-551
complementary angle measurements, $50,93,95,115,297$, 478, 485
cones, 550, 620, 632
cylinders, $320,546,551$
Fibonacci sequence, 824, 829
flag dimensions, 113
fraction representations in, 24-25,74
geodesic dome measurements, 115
golden rectangles, 116
hang glider dimensions, 429
Hoberman Sphere volume, 127
parallelograms, $15,113,127,138,320,363,368,432,515$
Pentagon floor space dimensions, 115, 463
pentagons, 105, 126
percent decrease/increase problems, 136, 138
perimeter, $25,35-36,74,86,104,105,122-123,126-127,157$,
$165,196,294,299,305,306,333,363,374,393,402,407,432$,
440, 441, 471, 477, 510, 546, 604, 625-626, 812, 873, 877
polygons, 546
Pythagorean theorem, 430-431, 636-638, 914
quadrilaterals, $96,114,299,300,432,440$
radius, 432, 532, 632
rectangles, $24,35-36,86,116,122-123,136,157,165,196$, $294,320,339,340,346,373,374,393,432,433,434,440$, 441, 464, 477, 625, 679, 873
sail dimensions, 126, 428-429, 440, 497, 515
sign dimensions, 120-121, 124, 125, 298, 877
spheres, 549, 555, 632
squares, $136,320,339,346,363,373,402,432,433,440$, 471, 670, 873
supplementary angle measurements, $50,93,95,115,297$, 478, 485
surface area, 321, 334, 372, 546, 555, 620, 640
trapezoids, 432, 471, 625, 626
triangles, $15,24,36,86,96,104,105,113,114,115,116$, $127,138,157,293,294,298,299,300,305,306,308,339$, 356, 374, 430-431, 432, 434, 440, 441, 442, 464, 490, 495, $498,511,512,514,604,625,639,641,649,670,679,717$, 824, 875, 876, 877, 913-914
Vietnam Veterans Memorial angle measurements, 109-110
volume, 36, 122, 127, 320, 321, 339, 356, 363, 368, 532, 550, 551, 632
Washington Monument height and base, 165
Government. See Politics \& Government

## H

Health \& Medicine
bacterial cultures, $828,834,841$
basal metabolic rate, 611
blinking rate of human eye, 116
body mass index, 454
body surface area of humans, 604
breast cancer pink ribbons, 127
cephalic index, 454
dog medicine dosages, 240, 532
flu epidemics, 778
fungal cultures, 841
hospital heights, 877
infectious diseases, 828
kidney transplants, 246
medication administration, $97,453,477$
octuplet birth weights, 74
organ transplants, 219, 246
pediatric dosages, 453, 477
radiation, 784
registered nurses, 192
smoking and pulse rate, 173
treadmills, 131
virus cultures, 836
woman's height given femur bone length, 240, 532
yeast cultures, 856,857
Home Improvement. See Construction \& Home Improvement

## I

Industry. See Business \& Industry
Insects. See Animals \& Insects

## M

Medicine. See Health \& Medicine

## N

Nutrition. See Food \& Nutrition

## P

Personal Finances
bank account balances, 47, 295, 649-650
bankruptcy, 514
charge account balances, 50
donations, 844-845
interest rates, $36,434,666-667,669,670,717,743,747,770$, $772-773,776,778,783,784,785,787,859,860$
loans, money needed to pay off, 321
money problems, 142-143
retirement party budgeting, 157
salary after pay raise, 136
salary growth, $832,836,841,848,856,857$
sales needed to ensure monthly salary, 166
savings accounts, $15,295,848$
wedding budget, $155,157,587$
Physics
angstroms, 373
angular frequency of oscillations, 612
currents and resistance, 549
Doppler effect, 505
Earth's interior temperature, 355
force exerted by tractors, 641
Hoberman Sphere volume, 127
horsepower, 550, 551
pendulum arc, $836,841,846,856,859$
pendulum period, 641
speed of waves traveling over stretched string, 612
springs stretching and Hooke's law, 543-544
velocity, 604, 658
weight of objects in relation to Earth's center, 549
wind power generated, 498
Politics \& Government
Democrats vs. Republicans, 109
governors, 109
mayoral elections, 95
national debts, 356
representatives, 109, 251
Supreme Court decisions, 138

## R

Real Estate
condominium sales and price relationships, 225
depreciation, 229
plot perimeter, 104
property values, 836
Recreation. See Entertainment \& Recreation

## S

Safety. See Transportation \& Safety
School. See Education
Space. See Astronomy \& Space
Sports
baseball earned run average, 505
baseball game admissions, 288
baseball game attendance, 260
baseball Hall of Fame admittance, 16
baseball payroll and team wins, 557
baseball runs batted in, 295
baseball slugging percentage, 454
baseball team wins, 877
basketball player heights, 157

Sports (continued)
basketball points scored, 295, 299-300
bowling average, 157
disc throwing records, 139
football stadiums, 876
football yards lost/gained, 61, 77
golf flags, 440
golf scores, 43, 58, 167
golf tournament participants, 749-750
hockey payrolls, 876
ice hockey penalty killing percentage, 477
NASCAR grandstand seats, 876
NASCAR speeds, 690
Olympics, 114, 461, 877
quarterback rating, 454
racquetball, 856
stock cars, 463
Super Bowl attendance, 182
Tour de France, 166

## T

Technology. See Communications \& Technology
Temperature \& Weather
atmospheric pressure, 747,778
average temperatures, 43, 51, 127, 234, 250
changes in, 40, 42, 50, 61, 77
Earth's interior temperature, 355
highest and lowest temperatures, 40, 42, 50, 127, 166, 680
inequality statements regarding, 15
of planets, 61
rainfall data, 300
snowfall at distances from Equator, 184
sunrise times, 233
sunset times, 238
temperature conversions, 119-120, 121, 123, 125, 127,
166, 567, 724
thermometer readings, 38
tornado classification, 168
tornadoes, 168, 874
Time \& Distance
airplane speed in still air, 296, 497, 498
bicycling speeds, 496, 688
bicycling travel time, 140, 296
boat speed in still water, $305,496,497,511,514$
boats traveling apart at right angles, 435
bus speeds, 145, 494, 497, 498
car speeds, 145, 493-494, 496, 497, 498, 511, 549, 640, 658
catamaran auto ferry speed, 125
comet distance from Earth, 355
conveyor belt speeds, 496
current speeds, 296, 305
Daytona 500 speeds, 690
distance saved, 675-676, 678-679, 720, 931
distance traveled over time, 166, 717
driving distance, 145
driving speeds, $36,146,493-494,496,497,498,685-686,688$
driving time, 125,127
dropped/falling objects, $35,228,325,331,372,376$, 413-414, 433, 434, 440, 441, 442, 524, 557, 641, 669-670, 676-677, 679-680, 828, 836, 846, 848, 856, 857
free-fall time/distance, 427, 848, 859
hiking trails, 25, 141, 308
hyenas overtaking giraffes, 499
hypersonic flight time around Earth, 128
jet vs. car distances, 497
lakes/ponds, distance across, 656, 800
light intensity by distance from source, 549, 550
light travel time/distance, 127-128, 356
moon's light to reach Earth, 357
motorcycle speeds, 498
objects traveling in opposite directions, 146, 168, 288-290, 297, 308, 496, 822, 930
of images and objects to focal length, 444
pendulum swings, $836,841,846,856,859$
rate and, 117-118
rope needed to wrap around Earth, 126
rowing against current, 496
rowing distance, 146
rowing rate in still water, 296
sight distance from a height, 549, 641
Sun's light to reach Earth, 357
thrown/launched objects, 393, 426, 433, 440, 697, 712-
$713,717,718,720,859,931$
traffic tickets, 146, 497
train travel speeds, $115,128,141-142,166,168,496,930$
travel time, 140-141
walking/running speeds, $305,496,688,691$
walking/running time, 166, 296, 305
wind speeds, 296, 496, 497, 498, 550
Transportation \& Safety
bridge lengths, 95
bridges, 220, 800, 822
bus speeds, 145, 494, 497, 498
car speeds, 145, 493-494, 496, 497, 498, 511, 549, 640, 658
catamaran auto ferry speed, 125
cell phone use while driving, 166
cloverleaf exits, 658
grade of roads/railroad tracks, 213, 217, 377
interstate highway length, 96
motorcycle speeds, 498
parking lot dimensions, 125
railroad tracks, 213, 217
road sign dimensions, 120-121, 125, 298, 377, 877
taxi cab fares, 586
traffic tickets, 146, 497
train fares for children and adults, 295
wheelchair ramps, 217
yield signs, 125

## V

Vehicles. See Automobiles

## W

Weather. See Temperature \& Weather

## Review of Real Numbers

### 1.1 Study Skill Tips for Success in Mathematics

1.2 Symbols and Sets of Numbers
1.3 Fractions and Mixed Numbers
1.4 Exponents, Order of Operations, Variable Expressions, and Equations
1.5 Adding Real Numbers

### 1.6 Subtracting Real Numbers Integrated Review-Operations on Real Numbers

### 1.7 Multiplying and Dividing Real Numbers

### 1.8 Properties of Real Numbers

## CHECK YOUR PROGRESS

Vocabulary Check
Chapter Highlights
Chapter Review
Getting Ready for the Test Chapter Test

In this chapter, we review the basic symbols and words-the language-of arithmetic and introduce using variables in place of numbers. This is our starting place in the study of algebra.

A Selection of Resources for Success in this Mathematics Course


Textbook


MyMathLab and MathXL


Instructor



For more information about the resources illustrated above, read Section 1.1.

### 1.1 Study Skill Tips for Success in Mathematics

## OBJECTIVES

1 Get Ready for This Course.
2 Understand Some General Tips for Success.
3 Know How to Use This Text. .

4 Know How to Use Text Resources.
5 Get Help as Soon as You Need It.
6 Learn How to Prepare for and Take an Exam.
7 Develop Good Time Management.

## Helpful Hint

MyMathLab $^{\circledR}$ and MathXL ${ }^{\circledR}$
When assignments are turned in online, keep a hard copy of your complete written work. You will need to refer to your written work to be able to ask questions and to study for tests later.

## Helpful Hint

## MyMathLab ${ }^{\circledR}$ and MathXL ${ }^{\circledR}$

If you are doing your homework online, you can work and re-work those exercises that you struggle with until you master them. Try working through all the assigned exercises twice before the due date.

Before reading Section 1.1, you might want to ask yourself a few questions.

1. When you took your last math course, were you organized? Were your notes and materials from that course easy to find, or were they disorganized and hard to find-if you saved them at all?
2. Were you satisfied-really satisfied-with your performance in that course? In other words, do you feel that your outcome represented your best effort?
If the answer is "no" to these questions, then it is time to make a change. Changing to or resuming good study skill habits is not a process you can start and stop as you please. It is something that you must remember and practice each and every day. To begin, continue reading this section.

## objective

## 1 Getting Ready for This Course

Now that you have decided to take this course, remember that a positive attitude will make all the difference in the world. Your belief that you can succeed is just as important as your commitment to this course. Make sure you are ready for this course by having the time and positive attitude that it takes to succeed.

Make sure that you are familiar with the way that this course is being taught. Is it a traditional course, in which you have a printed textbook and meet with an instructor? Is it taught totally online, and your textbook is electronic and you e-mail your instructor? Or is your course structured somewhere in between these two methods? (Not all of the tips that follow will apply to all forms of instruction.)

Also make sure that you have scheduled your math course for a time that will give you the best chance for success. For example, if you are also working, you may want to check with your employer to make sure that your work hours will not conflict with your course schedule.

On the day of your first class period, double-check your schedule and allow yourself extra time to arrive on time in case of traffic problems or difficulty locating your classroom. Make sure that you are aware of and bring all necessary class materials.

## objective

2 General Tips for Success
Below are some general tips that will increase your chance for success in a mathematics class. Many of these tips will also help you in other courses you may be taking.

- Most important! Organize your class materials. In the next couple pages, many ideas will be presented to help you organize your class materials - notes, any handouts, completed homework, previous tests, etc. In general, you MUST have these materials organized. All of them will be valuable references throughout your course and when studying for upcoming tests and the final exam. One way to make sure you can locate these materials when you need them is to use a three-ring binder. This binder should be used solely for your mathematics class and should be brought to each and every class or lab. This way, any material can be immediately inserted in a section of this binder and will be there when you need it.

Form study groups and/or exchange names and e-mail addresses. Depending on how your course is taught, you may want to keep in contact with your fellow students. Some ways of doing this are to form a study group - whether in person or through the Internet. Also, you may want to ask if anyone is interested in exchanging e-mail addresses or any other form of contact.

Choose to attend all class periods. If possible, sit near the front of the classroom. This way, you will see and hear the presentation better. It may also be easier for you to participate in classroom activities.

- Do your homework. You've probably heard the phrase "practice makes perfect" in relation to music and sports. It also applies to mathematics. You will find that the more time you spend solving mathematics exercises, the easier the process becomes. Be sure to schedule enough time to complete your assignments before the due date assigned by your instructor.


If you are completing your homework online, it's important to work each exercise on paper before submitting the answer. That way, you can check your work and follow your steps to find and correct any mistakes.

## Helpful Hint

MyMathLab ${ }^{\circledR}$ and MathXL ${ }^{\circledR}$
Be aware of assignments and due dates set by your instructor. Don't wait until the last minute to submit work online.

Check your work. Review the steps you took while working a problem. Learn to check your answers in the original exercises. You may also compare your answers with the "Answers to Selected Exercises" section in the back of the book. If you have made a mistake, try to figure out what went wrong. Then correct your mistake. If you can't find what went wrong, don't erase your work or throw it away. Show your work to your instructor, a tutor in a math lab, or a classmate. It is easier for someone to find where you had trouble if he or she looks at your original work.

Learn from your mistakes and be patient with yourself. Everyone, even your instructor, makes mistakes. (That definitely includes me-Elayn Martin-Gay.) Use your errors to learn and to become a better math student. The key is finding and understanding your errors.

Was your mistake a careless one, or did you make it because you can't read your own math writing? If so, try to work more slowly or write more neatly and make a conscious effort to carefully check your work.

Did you make a mistake because you don't understand a concept? Take the time to review the concept or ask questions to better understand it.

Did you skip too many steps? Skipping steps or trying to do too many steps mentally may lead to preventable mistakes.

Know how to get help if you need it. It's all right to ask for help. In fact, it's a good idea to ask for help whenever there is something that you don't understand. Make sure you know when your instructor has office hours and how to find his or her office. Find out whether math tutoring services are available on your campus. Check on the hours, location, and requirements of the tutoring service.

Don't be afraid to ask questions. You are not the only person in class with questions. Other students are normally grateful that someone has spoken up.

Turn in assignments on time. This way, you can be sure that you will not lose points for being late. Show every step of a problem and be neat and organized. Also be sure that you understand which problems are assigned for homework. If allowed, you can always double-check the assignment with another student in your class.

## OBJECTIVE

## 3 Knowing and Using Your Text

Flip through the pages of this text or view the e-text pages on a computer screen. Start noticing examples, exercise sets, end-of-chapter material, and so on. Every text is organized in some manner. Learn the way this text is organized by reading about and then finding an example in your text of each type of resource listed below. Finding and using these resources throughout your course will increase your chance of success.

- Practice Exercises. Each example in every section has a parallel Practice exercise. As you read a section, try each Practice exercise after you've finished the corresponding example. This "learn-by-doing" approach will help you grasp ideas before you move on to other concepts. Answers are at the back of the text.
- Symbols at the Beginning of an Exercise Set. If you need help with a particular section, the symbols listed at the beginning of each exercise set will remind you of the numerous resources available.
- Objectives. The main section of exercises in each exercise set is referenced by an example(s). There is also often a section of exercises entitled "Mixed Practice," which is referenced by two or more examples or sections. These are mixed exercises written to prepare you for your next exam. Use all of this referencing if you have trouble completing an assignment from the exercise set.
- Icons (Symbols). Make sure that you understand the meaning of the icons that are beside many exercises. O tells you that the corresponding exercise may be viewed on the video segment that corresponds to that section. \tells you that this exercise is a writing exercise in which you should answer in complete sentences. $\triangle$ tells you that the exercise involves geometry. 圈 tells you that this exercise is worked more efficiently with the aid of a calculator. Also, a feature called Graphing Calculator Explorations may be found before select exercise sets.


## Helpful Hint

## MyMathLab ${ }^{\text {® }}$

In MyMathLab, you have access to the following video resources:

- Lecture Videos for each section
- Chapter Test Prep Videos

Use these videos provided by the author to prepare for class, review, and study for tests.

- Integrated Reviews. Found in the middle of each chapter, these reviews offer you a chance to practice - in one place - the many concepts that you have learned separately over several sections.
- End-of-Chapter Opportunities. There are many opportunities at the end of each chapter to help you understand the concepts of the chapter.
Vocabulary Checks contain key vocabulary terms introduced in the chapter.
Chapter Highlights contain chapter summaries and examples.
Chapter Reviews contain review exercises. The first part is organized section by section and the second part contains a set of mixed exercises.
Getting Ready for the Tests contain conceptual exercises written to prepare students for chapter test directions as well as mixed sections of exercises.
Chapter Tests are sample tests to help you prepare for an exam. The Chapter Test Prep Videos found in the Interactive Lecture Series, MyMathLab, and YouTube provide the video solution to each question on each Chapter Test.
Cumulative Reviews start at Chapter 2 and are reviews consisting of material from the beginning of the book to the end of that particular chapter.
- Student Resources in Your Textbook. You will find a Student Resources section at the back of this textbook. It contains the following to help you study and prepare for tests:
Study Skills Builders contain study skills advice. To increase your chance for success in the course, read these study tips and answer the questions.
Bigger Picture-Study Guide Outline provides you with a study guide outline of the course, with examples.
Practice Final provides you with a Practice Final Exam to help you prepare for a final. The video solutions to each question are provided in the Interactive DVD Lecture Series and within MyMathLab ${ }^{\circledR}$.
- Resources to Check Your Work. The Answers to Selected Exercises section provides answers to all odd-numbered section exercises and all integrated review and chapter test exercises.


## objective

4 Knowing and Using Video and Notebook Organizer Resources

## Video Resources

Below is a list of video resources that are all made by me-the author of your text, Elayn Martin-Gay. By making these videos, I can be sure that the methods presented are consistent with those in the text.

- Interactive DVD Lecture Series. Exercises marked with a $\odot$ are fully worked out by the author on the DVDs and within MyMathLab. The lecture series provides approximately 20 minutes of instruction per section and is organized by Objective.
- Chapter Test Prep Videos. These videos provide solutions to all of the Chapter Test exercises worked out by the author. They can be found in MyMathLab, the Interactive Lecture series, and YouTube. This supplement is very helpful before a test or exam.
- Student Success Tips. These video segments are about 3 minutes long and are daily reminders to help you continue practicing and maintaining good organizational and study habits.
- Final Exam Videos. These video segments provide solutions to each question. These videos can be found within MyMathLab and the Interactive Lecture Series.


## Notebook Organizer Resource

This resource is in three-ring notebook ready form. It is to be inserted in a three-ring binder and completed. This resource is numbered according to the sections in your text to which they refer.

- Video Organizer. This organizer is closely tied to the Interactive Lecture (Video) Series. Each section should be completed while watching a lecture video on the same section. Once completed, you will have a set of notes to accompany the Lecture (Video) Series section by section.

\section*{| Helpful Hint |
| :--- |
| MyMathLab ${ }^{\circledR}$ and MathXL ${ }^{\circledR}$ |}

- Use the Help Me Solve This button to get step-by-step help for the exercise you are working. You will need to work an additional exercise of the same type before you can get credit for having worked it correctly.
- Use the Video button to view a video clip of the author working a similar exercise.


## Helpful Hint

MyMathLab ${ }^{\circledR}$ and MathXL ${ }^{\circledR}$
Review your written work for previous assignments. Then, go back and re-work previous assignments. Open a previous assignment, and click Similar Exercise to generate new exercises. Re-work the exercises until you fully understand them and can work them without help features.

## objective

## 5 Getting Help

If you have trouble completing assignments or understanding the mathematics, get help as soon as you need it! This tip is presented as an objective on its own because it is so important. In mathematics, usually the material presented in one section builds on your understanding of the previous section. This means that if you don't understand the concepts covered during a class period, there is a good chance that you will not understand the concepts covered during the next class period. If this happens to you, get help as soon as you can.

Where can you get help? Many suggestions have been made in this section on where to get help, and now it is up to you to get it. Try your instructor, a tutoring center, or a math lab, or you may want to form a study group with fellow classmates. If you do decide to see your instructor or go to a tutoring center, make sure that you have a neat notebook and are ready with your questions.

## objective

6 Preparing for and Taking an Exam
Make sure that you allow yourself plenty of time to prepare for a test. If you think that you are a little "math anxious," it may be that you are not preparing for a test in a way that will ensure success. The way that you prepare for a test in mathematics is important. To prepare for a test:

1. Review your previous homework assignments.
2. Review any notes from class and section-level quizzes you have taken. (If this is a final exam, also review chapter tests you have taken.)
3. Review concepts and definitions by reading the Chapter Highlights at the end of each chapter.
4. Practice working out exercises by completing the Chapter Review found at the end of each chapter. (If this is a final exam, go through a Cumulative Review. There is one found at the end of each chapter except Chapter 1 . Choose the review found at the end of the latest chapter that you have covered in your course.) Don't stop here!
5. It is important that you place yourself in conditions similar to test conditions to find out how you will perform. In other words, as soon as you feel that you know the material, get a few blank sheets of paper and take a sample test. There is a Chapter Test available at the end of each chapter, or you can work selected problems from the Chapter Review. Your instructor may also provide you with a review sheet. During this sample test, do not use your notes or your textbook. Then check your sample test. If your sample test is the Chapter Test in the text, don't forget that the video solutions are in MyMathLab, the Interactive Lecture Series, and YouTube. If you are not satisfied with the results, study the areas that you are weak in and try again.
6. On the day of the test, allow yourself plenty of time to arrive where you will be taking your exam.
When taking your test:
7. Read the directions on the test carefully.
8. Read each problem carefully as you take the test. Make sure that you answer the question asked.
9. Watch your time and pace yourself so that you can attempt each problem on your test.
10. If you have time, check your work and answers.
11. Do not turn your test in early. If you have extra time, spend it double-checking your work.


## objective

7 Managing Your Time
As a college student, you know the demands that classes, homework, work, and family place on your time. Some days you probably wonder how you'll ever get everything done. One key to managing your time is developing a schedule. Here are some hints for making a schedule:

1. Make a list of all your weekly commitments for the term. Include classes, work, regular meetings, extracurricular activities, etc. You may also find it helpful to list such things as laundry, regular workouts, grocery shopping, etc.
2. Next, estimate the time needed for each item on the list. Also make a note of how often you will need to do each item. Don't forget to include time estimates for the reading, studying, and homework you do outside of your classes. You may want to ask your instructor for help estimating the time needed.
3. In the exercise set that follows, you are asked to block out a typical week on the schedule grid given. Start with items with fixed time slots like classes and work.
4. Next, include the items on your list with flexible time slots. Think carefully about how best to schedule items such as study time.
5. Don't fill up every time slot on the schedule. Remember that you need to allow time for eating, sleeping, and relaxing! You should also allow a little extra time in case some items take longer than planned.
6. If you find that your weekly schedule is too full for you to handle, you may need to make some changes in your workload, classload, or other areas of your life. You may want to talk to your advisor, manager or supervisor at work, or someone in your college's academic counseling center for help with such decisions.

### 1.1 Exercise Set MyMathLab ${ }^{(D)}$

1. What is your instructor's name?
2. What are your instructor's office location and office hours?
3. What is the best way to contact your instructor?
4. Do you have the name and contact information of at least one other student in class?
5. Will your instructor allow you to use a calculator in this class?
6. Why is it important that you write step-by-step solutions to homework exercises and keep a hard copy of all work submitted?
7. Is there a tutoring service available on campus? If so, what are its hours? What services are available?
8. Have you attempted this course before? If so, write down ways that you might improve your chances of success during this next attempt.
9. List some steps that you can take if you begin having trouble understanding the material or completing an assignment. If you are completing your homework in MyMathLab ${ }^{\circledR}$ and Math $\mathrm{XL}^{\circledR}$, list the resources you can use for help.
10. How many hours of studying does your instructor advise for each hour of instruction?
11. What does the icon in this text mean?
12. What does the $\triangle$ icon in this text mean?
13. What does the icon in this text mean?
14. What are Practice exercises?
15. When might be the best time to work a Practice exercise?
16. Where are the answers to Practice exercises?
17. What answers are contained in this text and where are they?
18. What are Study Skills Builders and where are they?
19. What and where are Integrated Reviews?
20. How many times is it suggested that you work through the homework exercises in MathXL ${ }^{\circledR}$ before the submission deadline?
21. How far in advance of the assigned due date is it suggested that homework be submitted online? Why?
22. Chapter Highlights are found at the end of each chapter. Find the Chapter 1 Highlights and explain how you might use it and how it might be helpful.
23. Chapter Reviews are found at the end of each chapter. Find the Chapter 1 Review and explain how you might use it and how it might be useful.
24. Chapter Tests are at the end of each chapter. Find the Chapter 1 Test and explain how you might use it and how it might be helpful when preparing for an exam on Chapter 1. Include how the Chapter Test Prep Videos may help. If you are working in MyMathLab ${ }^{\circledR}$ and MathXL ${ }^{\circledR}$, how can you use previous homework assignments to study?
25. What is the Video Organizer? Explain the contents and how it might be used.
26. Explain how the Video Organizer can help you when watching a lecture video.
27. Read or reread Objective 7 and fill out the schedule grid below.

|  | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1:00 a.m. |  |  |  |  |  |  |  |
| 2:00 a.m. |  |  |  |  |  |  |  |
| 3:00 a.m. |  |  |  |  |  |  |  |
| 4:00 a.m. |  |  |  |  |  |  |  |
| 5:00 a.m. |  |  |  |  |  |  |  |
| 6:00 a.m. |  |  |  |  |  |  |  |
| 7:00 a.m. |  |  |  |  |  |  |  |
| 8:00 a.m. |  |  |  |  |  |  |  |
| 9:00 a.m. |  |  |  |  |  |  |  |
| 10:00 a.m. |  |  |  |  |  |  |  |
| 11:00 a.m. |  |  |  |  |  |  |  |
| No0n |  |  |  |  |  |  |  |
| 1:00 p.m. |  |  |  |  |  |  |  |
| 2:00 p.m. |  |  |  |  |  |  |  |
| 3:00 p.m. |  |  |  |  |  |  |  |
| 4:00 p.m. |  |  |  |  |  |  |  |
| 5:00 p.m. |  |  |  |  |  |  |  |
| 6:00 p.m. |  |  |  |  |  |  |  |
| 7:00 p.m. |  |  |  |  |  |  |  |
| 8:00 p.m. |  |  |  |  |  |  |  |
| 9:00 p.m. |  |  |  |  |  |  |  |
| 10:00 p.m. |  |  |  |  |  |  |  |
| 11:00 p.m. |  |  |  |  |  |  |  |
| Midnight |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

### 1.2 Symbols and Sets of Numbers

## OBJECTIVES

1 Use a Number Line to Order Numbers.
2 Translate Sentences into Mathematical Statements.
3 Identify Natural Numbers, Whole Numbers, Integers, Rational Numbers, Irrational Numbers, and Real Numbers.
4 Find the Absolute Value of a Real Number.


A Number Line


## objective

1 Using a Number Line to Order Numbers
We begin with a review of the set of natural numbers and the set of whole numbers and how we use symbols to compare these numbers. A set is a collection of objects, each of which is called a member or element of the set. A pair of brace symbols $\}$ encloses the list of elements and is translated as "the set of" or "the set containing."

| Natural Numbers <br> The set of natural numbers is $\{1,2,3,4,5,6, \ldots\}.$. | Helpful Hint <br> The three dots (an <br> ellipsis) means that <br> the list continues in <br> the same manner <br> indefinitely. |
| :--- | :--- |
| Whole Numbers |  |

These numbers can be pictured on a number line. We will use number lines often to help us visualize distance and relationships between numbers.

To draw a number line, first draw a line. Choose a point on the line and label it 0. To the right of 0 , label any other point 1 . Being careful to use the same distance as from 0 to 1 , mark off equally spaced distances. Label these points $2,3,4,5$, and so on. Since the whole numbers continue indefinitely, it is not possible to show every whole number on this number line. The arrow at the right end of the line indicates that the pattern continues indefinitely.

Picturing whole numbers on a number line helps us see the order of the numbers. Symbols can be used to describe concisely in writing the order that we see.

> The equal symbol $=$ means "is equal to."
> The symbol $\neq$ means "is not equal to."

These symbols may be used to form a mathematical statement. The statement might be true or it might be false. The two statements below are both true.

$$
\begin{array}{ll}
2=2 & \text { states that "two is equal to two." } \\
2 \neq 6 & \text { states that "two is not equal to six." }
\end{array}
$$

If two numbers are not equal, one number is larger than the other.
The symbol > means "is greater than."
The symbol $<$ means "is less than." For example,

$$
\begin{array}{ll}
3<5 & \text { states that "three is less than five." } \\
2>0 & \text { states that "two is greater than zero." }
\end{array}
$$

On a number line, we see that a number to the right of another number is larger. Similarly, a number to the left of another number is smaller. For example, 3 is to the left of 5 on a number line, which means that 3 is less than 5 , or $3<5$. Similarly, 2 is to the right of 0 on a number line, which means 2 is greater than 0 , or $2>0$. Since 0 is to the left of 2 , we can also say that 0 is less than 2 , or $0<2$.

The symbols $\neq,<$, and $>$ are called inequality symbols.

## Helpful Hint

Notice that $2>0$ has exactly the same meaning as $0<2$. Switching the order of the numbers and reversing the direction of the inequality symbol does not change the meaning of the statement.

$$
3<5 \text { has the same meaning as } 5>3
$$

Also notice that, when the statement is true, the inequality arrow points to the smaller number.

EXAMPLE I Insert $<,>$, or $=$ in the space between each pair of numbers to make each statement true
a. 23
b. 74
c. $72 \quad 27$

## Solution

a. $2<3$ since 2 is to the left of 3 on a number line.
b. $7>4$ since 7 is to the right of 4 on a number line.
c. $72>27$ since 72 is to the right of 27 on a number line.

## PRACtICE

1 Insert $<,>$, or $=$ in the space between each pair of numbers to make each statement true.
a. 58
b. 64
c. 16
82

Two other symbols are used to compare numbers.
The symbol $\leq$ means "is less than or equal to."
The symbol $\geq$ means "is greater than or equal to." For example,
$7 \leq 10$ states that "seven is less than or equal to ten."
This statement is true since $7<10$ is true. If either $7<10$ or $7=10$ is true, then $7 \leq 10$ is true.

$$
3 \geq 3 \text { states that "three is greater than or equal to three." }
$$

This statement is true since $3=3$ is true. If either $3>3$ or $3=3$ is true, then $3 \geq 3$ is true.

The statement $6 \geq 10$ is false since neither $6>10$ nor $6=10$ is true. The symbols $\leq$ and $\geq$ are also called inequality symbols.

EXAMPLE 2 Tell whether each statement is true or false.
a. $8 \geq 8$
b. $8 \leq 8$
c. $23 \leq 0$
d. $23 \geq 0$

## Solution

a. True. Since $8=8$ is true, then $8 \geq 8$ is true.
b. True. Since $8=8$ is true, then $8 \leq 8$ is true.
c. False. Since neither $23<0$ nor $23=0$ is true, then $23 \leq 0$ is false.
d. True. Since $23>0$ is true, then $23 \geq 0$ is true.

## PRACTICE

2 Tell whether each statement is true or false.
a. $9 \geq 3$
b. $3 \geq 8$
c. $25 \leq 25$
d. $4 \leq 14$

## objective

2 Translating Sentences


Now, let's use the symbols discussed to translate sentences into mathematical statements.

## EXAMPLE 3 Translate each sentence into a mathematical statement.

a. Nine is less than or equal to eleven.
b. Eight is greater than one.
c. Three is not equal to four.

